

## **Multi resolution defect transformation of the crack under different angles**

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**ABSTRACT :** *It is used to analyze the crack of different angles by the method of finite element. In the same material, the same crack is applied different angles, crack with 15 degree Angle differences, and applying I type load on the material. The effective elastic modulus under the different angles of crack are obtained by finite element. With comparative judgment method, it provides the relationship between the modulus of elasticity and crack different angles, and a method crack material defects of transformation. On based on the transformation of energy equivalent principle, there are a lot of crack defects of materials for different degrees of defects, so as to simplify the material crack, provide a simple way for material fatigue analysis.*

**Keywords** –multiresolution;material defect;elasticity modulus

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### **I. INTRODUCTION**

The most parts in mechanical engineering are under cyclic loading, so the cycle load is a major cause of leading to fatigue damage. In general, for high cyclic fatigue, Material of stress level is far less than the yield strength of its own and therefore fatigue damage of sudden, so often with huge property losses and casualties. There are two main types of research method of fatigue life, the kind of research method is based on damage mechanics and fracture mechanics; Another is to use s-n curve to predict the fatigue life. The former could not accurately the fatigue process of material defects, so the feasibility is poor; the latter need to do a lot of fatigue life test, wasting time and energy. The new method for fatigue life prediction of mainly on the material defects to simplify classification. For example, The GongL, Beijing University of Technology, on the labview platform is presented in this paper. a intelligent recognition system of defects, but the accuracy is not high; Xue-zhi Yang, hefei industrial university, China put forward a minimum classification error small potter of the textile defects classification research, but this method mainly is in textiles, limitations. At the university of Michigan, ShenJie, different defect levels of transformation method is put forward, Mainly for the approximation of the triangle, circle, square defects., using the finite element simulation and numerical analysis method to the simplification of different levels of defects. However, no study of crack configuration of different angles, this paper mainly aims at this problem, the different point of view of limited analysis of crack, determine the crack under different angle of effective elastic modulus of the material.

### **II. MULTIRESONTION MOTHEDS**

#### **2.1The defect of multiresolution transformation**

In practical engineering, there are a large number of defects for after long-term working components, the main defects as crack, distribution of irregularity. These cracks distributed from microscopic to macroscopicIn order to realize the material,multi-resolution damage method need an equivalent transformation method, makes different levels of material defects contact with each other, and find the effective elastic modulus of materials where there is injury.Taking the properties of the material in the cyclic loading into consideration. Transformation rules of material defects are shown in Figure 1, assumes that the material has all sorts of different levels of flaw, in one way, the first to use material of the initial elastic modulus E0. Step by step to estimate the damage of material, the effective elastic modulus of E1was finally determined. Again on the basis of the effective elastic modulus of E1,it is estimatedfor the material damage of secondary cracks, eventually to determine the effective elastic modulus of E2. Another method, on the basis of the original all defects, and estimate the damage of materials, directly in the original are determined on the basis of elastic modulus E0 material effective elastic modulus of E3.

Eventually it is determined for the elastic modulus of E2 and E3, respectively under the two kinds of methods to find the effective young's modulus. We also need compare the gap between the two

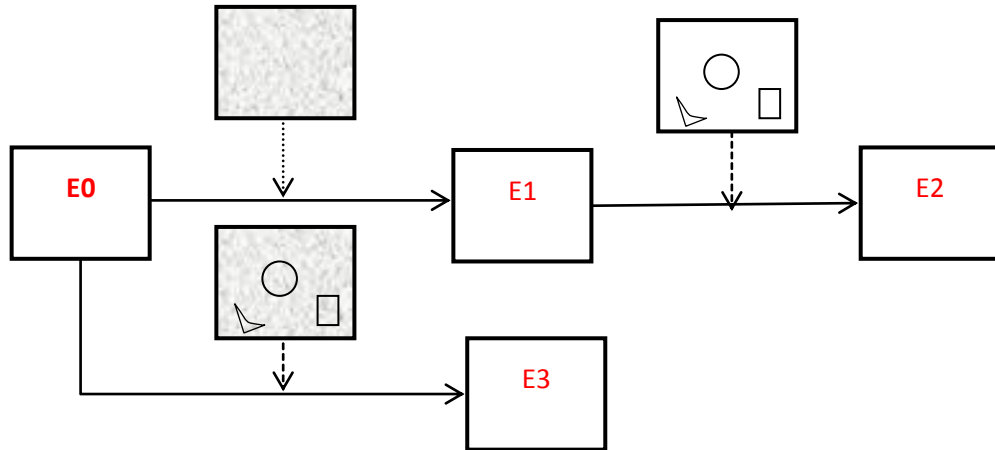


Fig. 1 defects into law

### 2.2 Numerical analysis of multi resolution

The above example is only two levels of the classification of the crack under simplified, whether classify can simplify between cracks, the heaviest is that if damage conversion is effective. The most crucial step is that a multi-scale damage mechanics model is set up. We assume that: the different levels of complementary energy of elastic mechanics modelis expressed by the following

$$W^e(\sigma_{D_i}, D_i) = \frac{1}{2} \sigma_{D_i}^T : \tilde{C}_{D_i}^{-1} : \sigma_{D_i}, \quad i = 0, 1, \dots, n \quad (1)$$

$W^e()$ ——a complementary elastic energy,

$D_i$ ——a damagetensor that represents the extent of damage accumulated from level 1 to level $i$ ,

$T$ ——the transpose of a matrix,

$\sigma_{D_i}$ ——a stresstensor at damage $D_i$ ,

$\tilde{C}_{D_i}^{-1}$ ——the inverse of an effective stiffnesstensor,

There is the following special case:in which $C^{-1}$ is the inverse of a stiffness tensor at damage  $D_0=0$ .  $\tilde{C}_{D_i}^{-1} =$

$$C^{-1}, \quad (2)$$

We also assume that the equivalence of complementary energy takes thefollowing incremental form:

$$\begin{aligned} W^e(\sigma_{D_{i+1}}, D_{i+1}) &= W^e(\sigma_{D_{i+1}}, D_i) \\ &= \frac{1}{2} \tilde{\sigma}_{D_{i+1}}^T : \tilde{C}_{D_i}^{-1} : \tilde{\sigma}_{D_{i+1}} \\ &= \frac{1}{2} \tilde{\sigma}_{D_i}^T : \left( M(dD_i)^T : \tilde{C}_{D_i}^{-1} : M(dD_i) \right) : \tilde{\sigma}_{D_i} \end{aligned} \quad (3)$$

$\tilde{\sigma}_{D_{i+1}}$ ——The effective stress tensor in the  $D_{i+1}$ , To solve the equations as follows:

$$\tilde{\sigma}_{D_{i+1}} = M(dD_i) : \tilde{\sigma}_{D_i}, \quad (4)$$

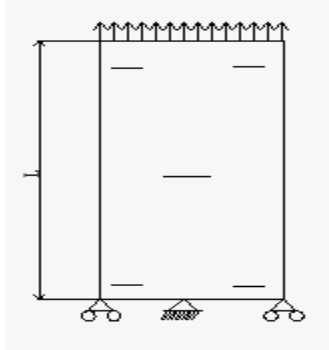
$$dD_i = D_{i+1} - D_i, \quad i = 0, 1, \dots, n - 1 \quad (5)$$

The equation expressed the material defect of multi-resolution transformation rules. It is mainly used for the different levels material defects to be homogeneously processed.

## III. FINITE ELEMENT ANALYSIS OF CRACK DEFECT DISCUSSION

### 3.1 Sample simulation parameters

The finite element software is used in the simulation of ABAQUS, and the stress singularity at the crack tip of ABAQUS has a strong analytical ability, which can show the crack propagation phenomenon. The specific parameters of the sample are shown in Table 1

	Table 1	The simulation test specimen		
Parameter	Data			
Specimen size (L×B)	100×40 (mm)			
Applying external force (kPa)	100			
Crack sizes (L)	10 (mm)			
Crack angle (degree)	15			
Elasticity modulus	$3 \times 10^7$			
Poisson ratio	0.3			

**3.2 Analysis and calculation of elastic modulus in finite element method**

This Due to the material itself inherent attributes, there are some inevitable defects on materials. In the machining process of parts, there are different length and arrangement of cracks. As shown in the following diagram: the crack is rotated counterclockwise, and the angle of each rotation is 15 degrees, and the straight line between the figures is preset. Boundary conditions: The sample boundary in the direction of Y axis is fixed, allowing the displacement in the X axis direction. The stress and strain are solved under different conditions. Due to the limitations of the finite element software, we can only get the stress or strain of a single node or element, so we need to solve the average stress and average strain of the whole material.

$$\bar{\sigma} = \frac{F_1 + F_2 + \dots}{A} \quad (6)$$

$$\bar{\epsilon} = \frac{(d_1 - d_3) + (d_2 - d_4) + \dots}{nL} \quad (7)$$

$\bar{\sigma}$  : mean stress,

$\bar{\epsilon}$  : mean strain,

$F_i$  : the force of node i,

n : node number,

**3.3 Calculation results and discussion of elastic modulus**

Finite element software can be on the structure of stress and strain analysis, using the finite element software general after pre-processing, solution and post treatment process by visualization module in the post processing of the extracted n nodes stress and displacement components, to approximately calculate the presence of different defects of the elastic modulus of materials. The specific analysis process as shown in Figure2

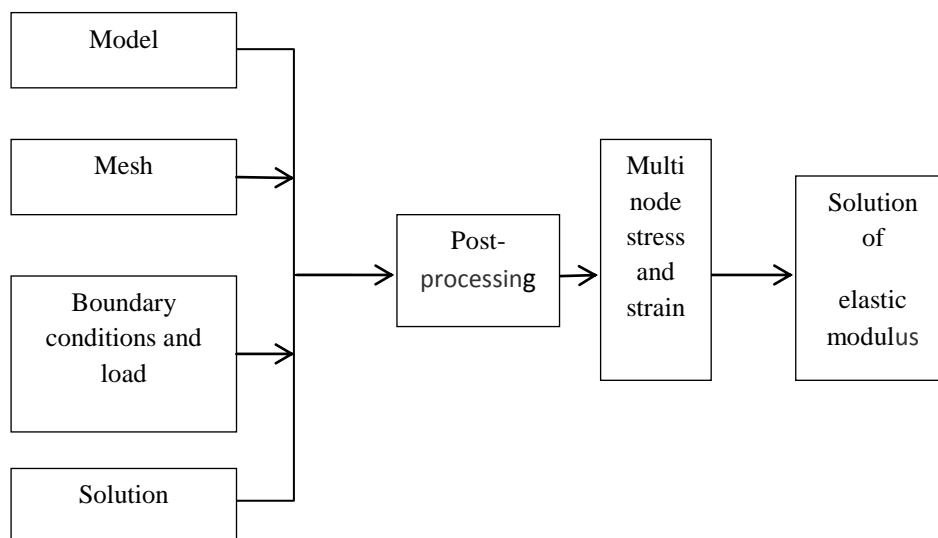
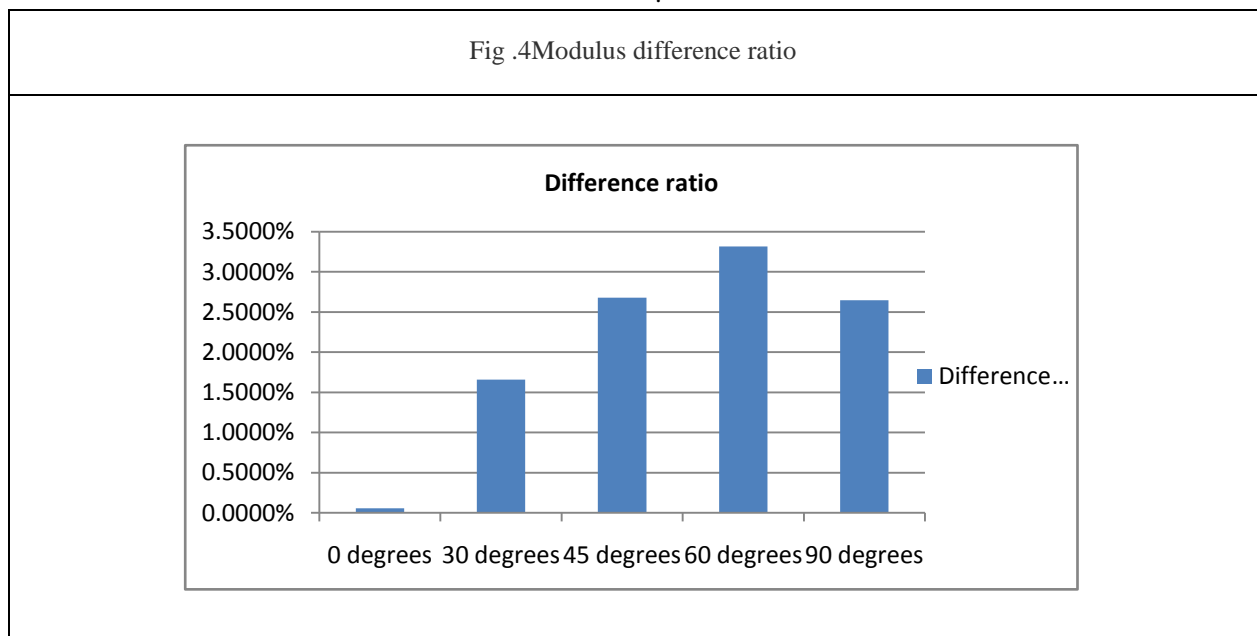
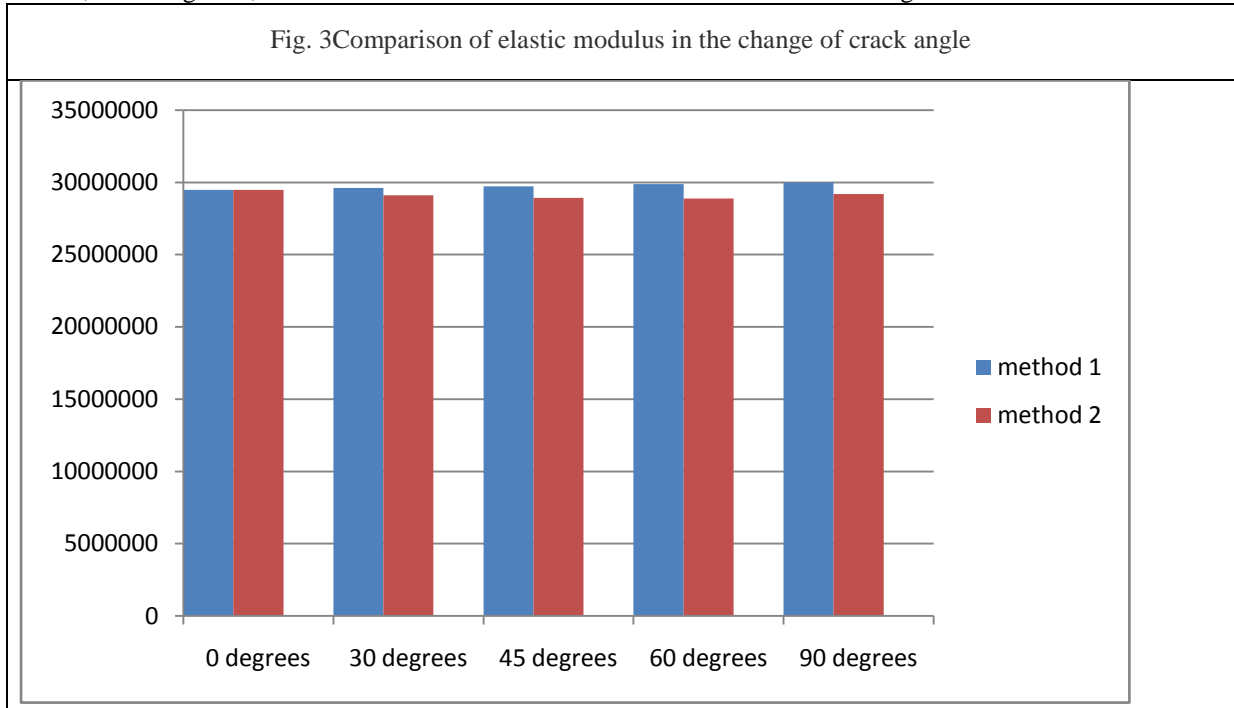


Fig. 2 Analysis of elastic modulus in finite element method

It in Figure 3 shows values for the elastic modulus under different angles, wherein E1 represents a crack perpendicular to the external load, E2 load and crack angle is 15 degrees, and so on. From the table available, when cracks are present at different angles, the elastic modulus of gradual change. Perpendicular to the crack and the external load and change of its elastic modulus value maximum, the influence on the properties of materials maximum. With the increase of the angle, trend of elastic modulus decreases, finally tends to be stable, From Figure 4, the difference in elastic modulus is within the allowable range of 10%



#### IV. CONCLUSION

For fatigue analysis, due to the irregularity of the crack, it is almost impossible to adopt accurate classification of crack. Finite element simulation through the cracks of different angle, we can summarize influence of edge crack of elastic modulus is greater than the median crack; influence of cracks on the elastic modulus is greater than a single crack; crack in different angles, elastic modulus with the change. The vertical

effects of the elastic modulus of the material to a load of the crack. It has important significance for predicting fatigue life and the simplified finite element model.

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